

**A derivation of optimum coherent Digital Elevation Models from
interferometric SAR data**

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Results obtained from application of fully Polarimetric Classification and Interferometric Parameter estimation algorithms onto GlenAffric L-band radar data are presented.

- Estimation of Interferogram from high resolution Parameter Estimation algorithm (ESPRIT)
- Despeckled Interferogram (Edge aligned Lee Filter)
- Digital Elevation Model based on local Region Grow algorithm

GlenAffric Test Site



Test Site

GlenAffric in
Scotland

Holds one of the
Largest & Oldest
Semi-Natural
Caledonian Pine forests

Typical species
Scots Pines

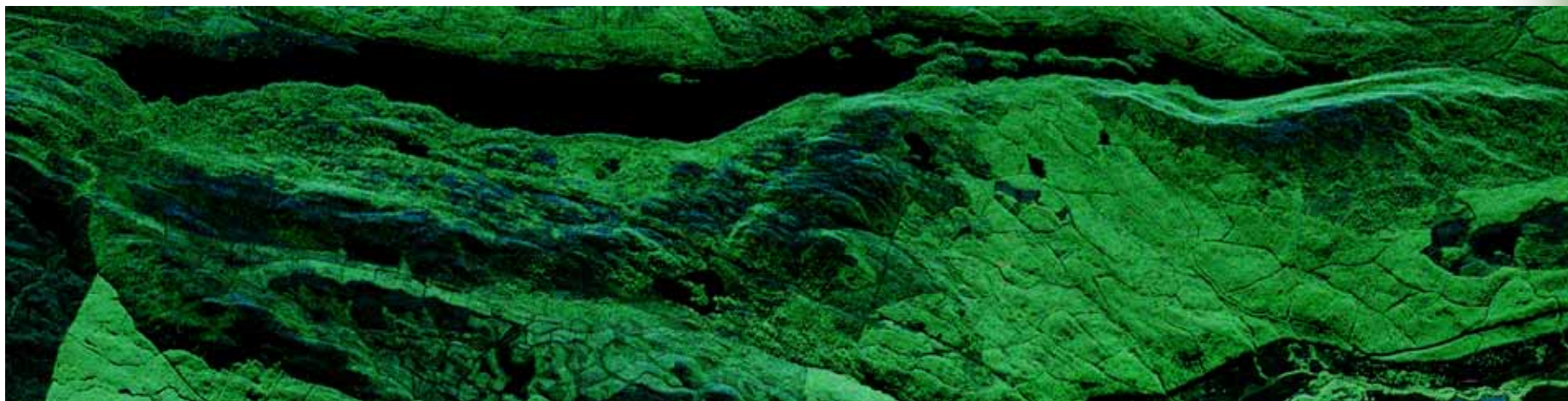
Topographically
Challenging site

Vast areas of
Peat/Heather lands and
Woodlands





Radar Data



RGB Image of Glenaffric SAR Data- Pauli Decomposition

Even Bounce

Tilted Even Bounce

Odd Bounce



● Acquired as part of the Scottish-SHAC

in April 2000,

Airborne, Repeat pass,

Fully Polarimetric

Dual Base Line,

L Band SAR data

With Baselines 10&20m

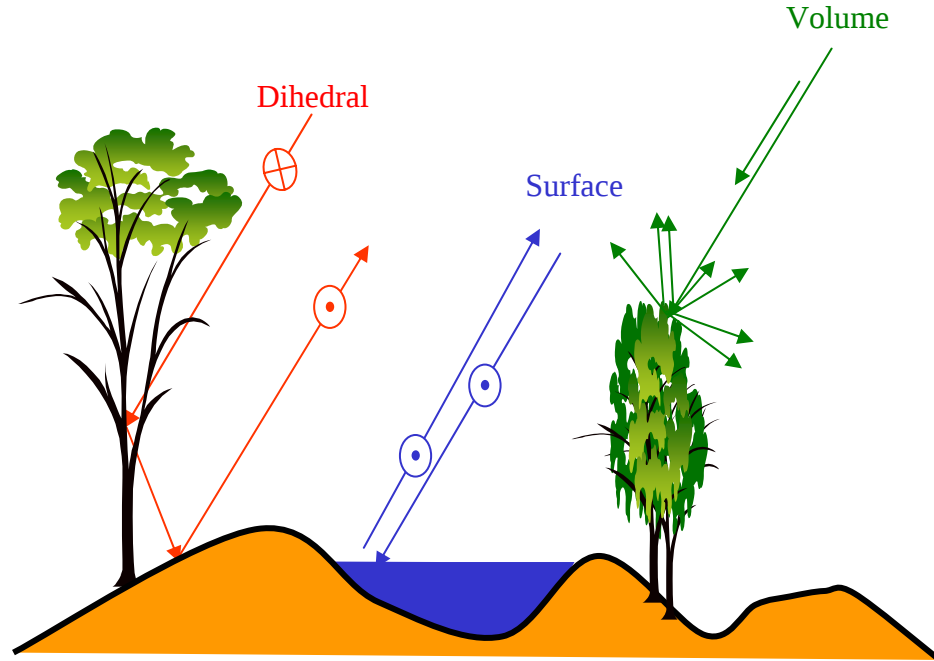
Total of 6 Tracks

SHAC info web-site :

<http://www.bnsc.gov.uk>

Land Cover Classification

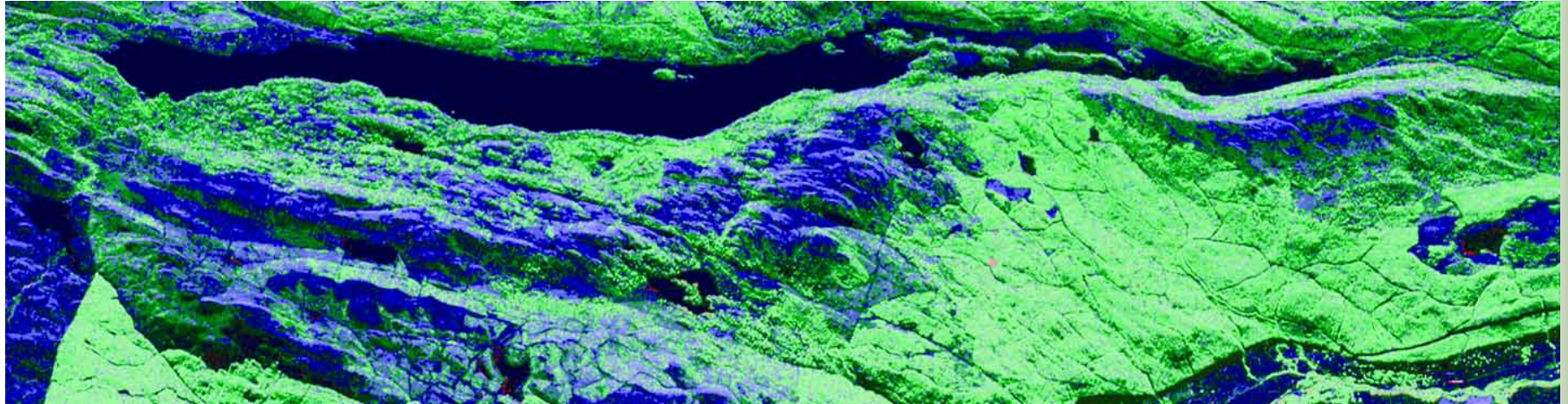
Freeman-Durden 3D Component Classification of



$$\mathbf{T} = \mathbf{T}_v + \mathbf{T}_s + \mathbf{T}_d$$

$$T_v = 4/3 \cdot m_v \cdot \begin{bmatrix} 2 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}; T_s = m_s \cdot \begin{bmatrix} (y+1)^2 & (y^2-1) & 0 \\ (y^2-1)^* & (y-1)^2 & 0 \\ 0 & 0 & 0 \end{bmatrix}; \text{ and } T_d = m_d \cdot \begin{bmatrix} (x-1)^2 & (x^2-1) & 0 \\ (x^2-1)^* & (x+1)^2 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Land Cover Classification



Freeman-Durden

3D Component
Classification of
Glenaffric radar data

The Freeman classified Glen Affric radar data



Estimation of Parameters via Rotational Invariance Techniques (ESPRIT)

$$\text{Interferometric Target vector} = \mathbf{S} = \begin{bmatrix} S_{HH_1} & S_{HV_1} & S_{VV_1} & S_{VH_1} & S_{HH_2} & S_{HV_2} & S_{VV_2} & S_{VH_2} \end{bmatrix}^T$$

$$\text{Covariance Matrix} = \mathbf{C}_{8 \times 8} = \mathbf{S} \mathbf{S}^* = \mathbf{E} \mathbf{\Lambda}_c \mathbf{E}^*, \quad \mathbf{E} = [\mathbf{E}_s, \mathbf{E}_n]$$

$$\mathbf{E}_s = \begin{bmatrix} \mathbf{E}_1 \\ \mathbf{E}_2 \end{bmatrix}, \quad \mathbf{E}_2 = \Phi \cdot \mathbf{E}_1$$

$$\text{TLS ESPRIT } \mathbf{E}_{12} = [\mathbf{E}_1, \mathbf{E}_2]$$

$$\mathbf{E}_{12}^* \cdot \mathbf{E}_{12} = \mathbf{G} \mathbf{\Lambda}_G \mathbf{G}^*$$

$$\mathbf{G} = \begin{bmatrix} [G_{1s}] & [G_{1n}] \\ [G_{2s}] & [G_{2n}] \end{bmatrix}$$

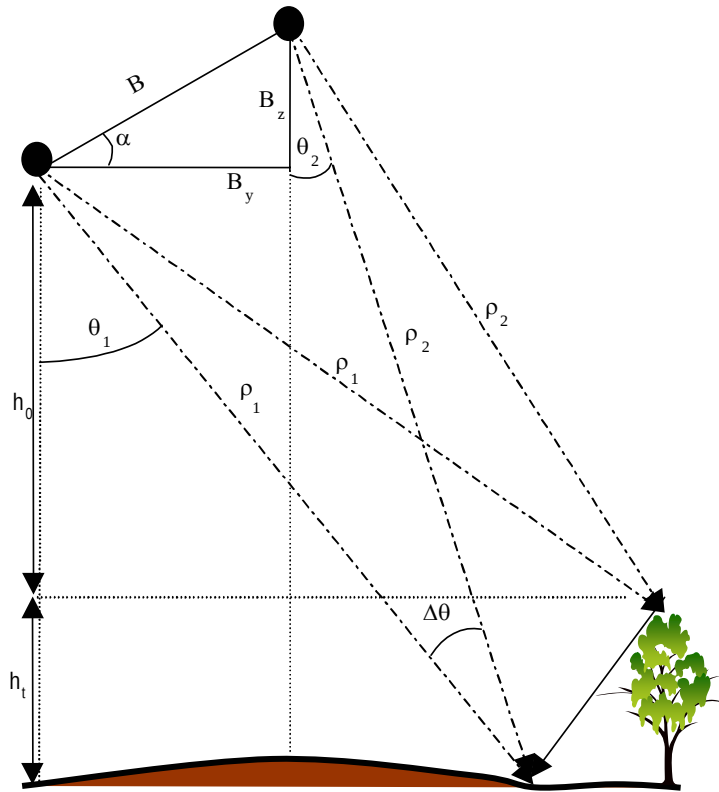
$$\psi = -\mathbf{G}_{1n} \cdot (\mathbf{G}_{2n})^{-1}, \quad \Phi = \arg(\text{Eigen values of } \psi)$$

$\Delta\Phi$ = Phase difference

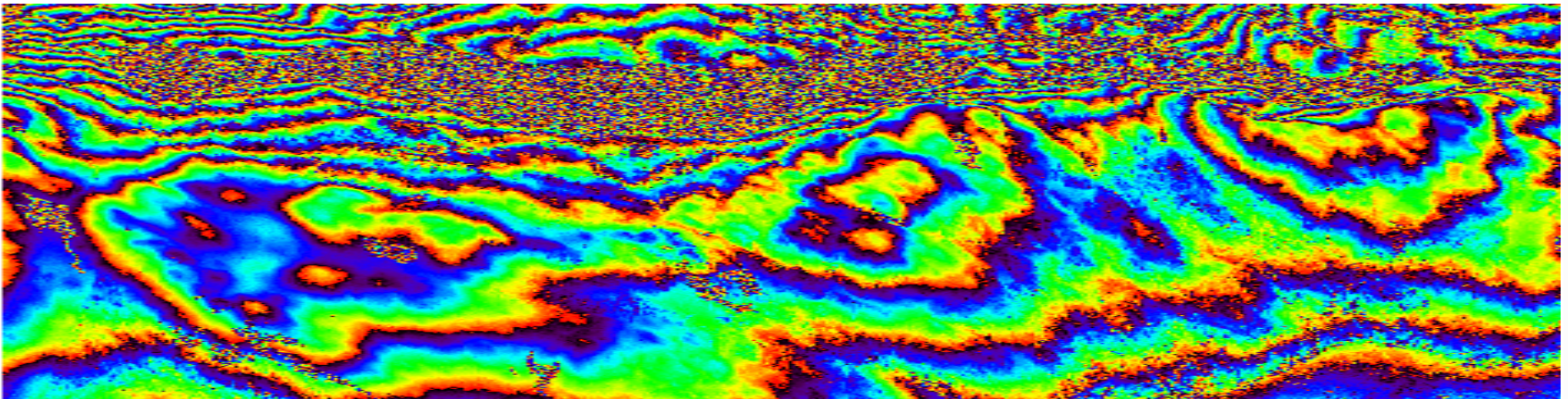
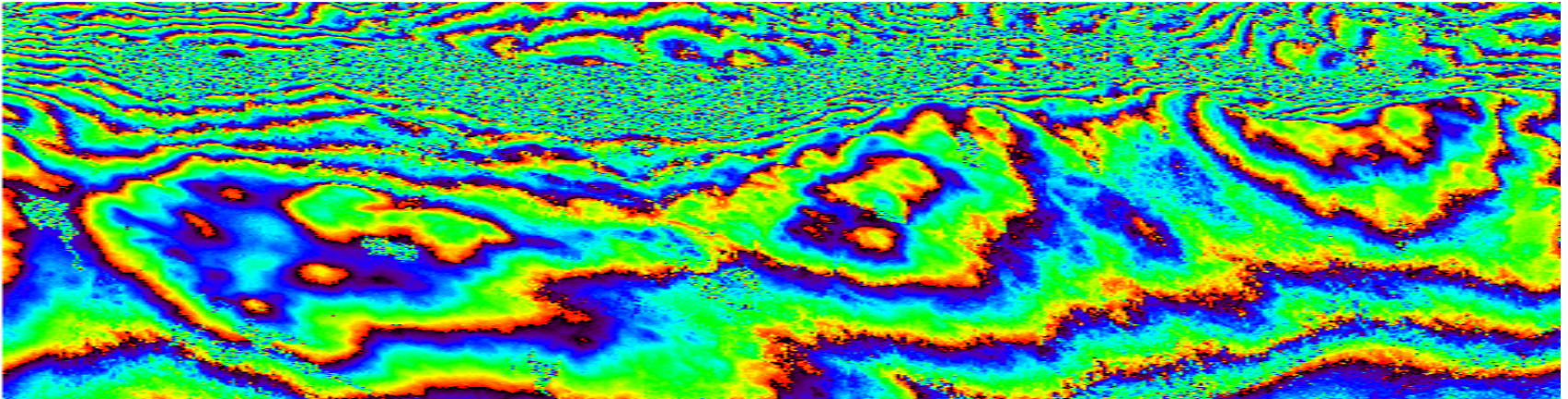
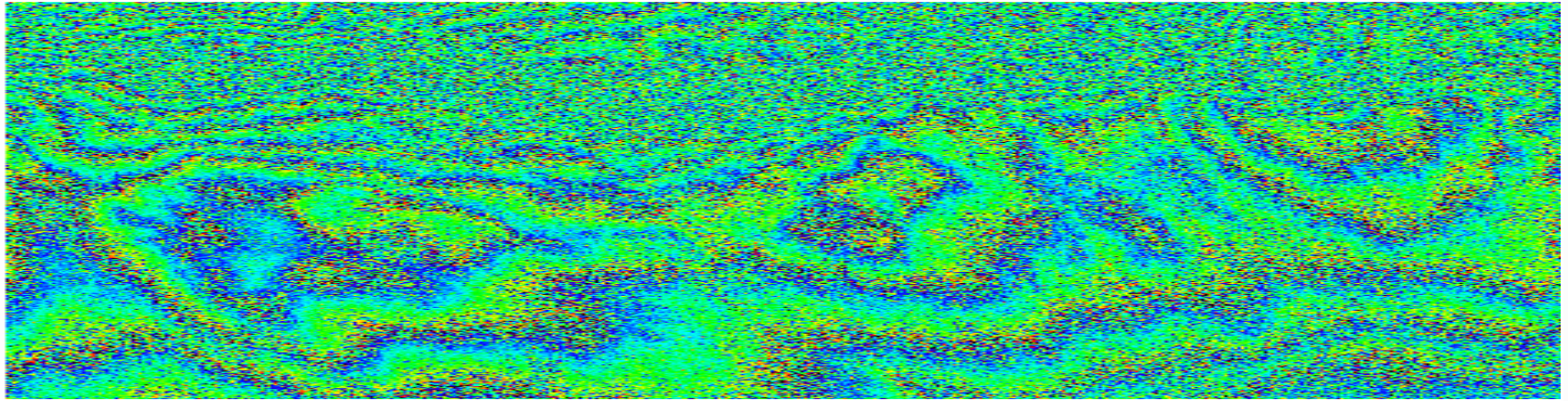
$$\text{Path difference} = \Delta\rho = \rho_1 - \rho_2$$

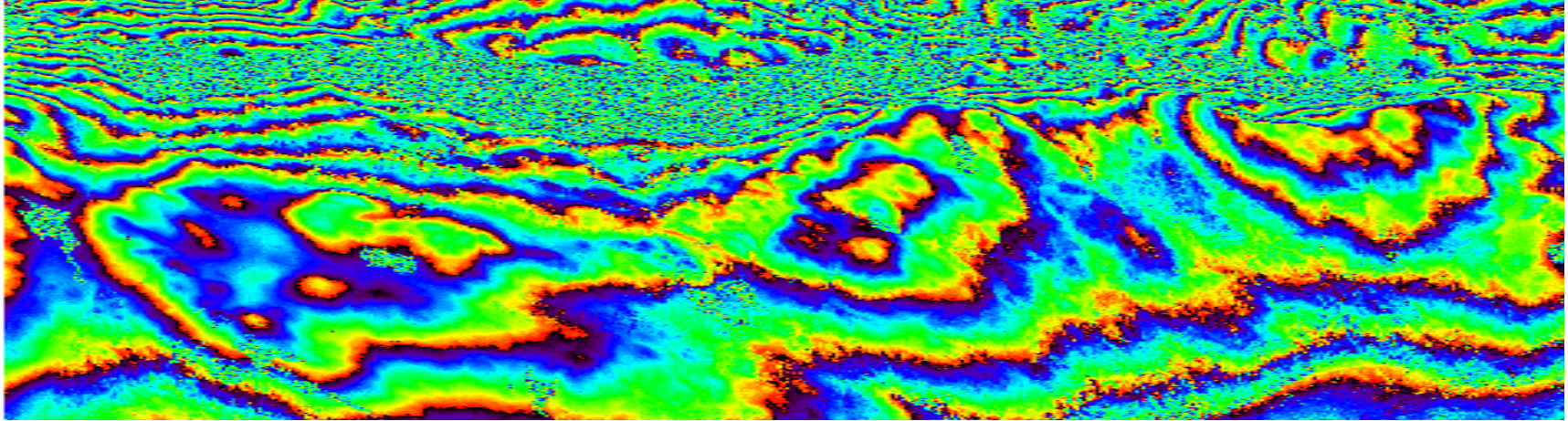
$$\text{Phase difference} = \frac{4\pi \Delta\rho}{\lambda} = \frac{4\pi}{\lambda} \cdot \Delta\theta \cdot \frac{h_t}{\sin(\theta_0)}$$

$$\text{Tree height} = h_t = \Delta\phi / (\sin(\theta_0) \lambda / (4\pi \Delta\theta))$$



Interferogram maps



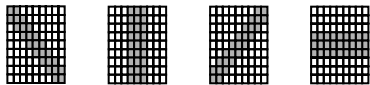


Augmented Coherence matrix

Classified Information

Dividing the image into three scattering groups

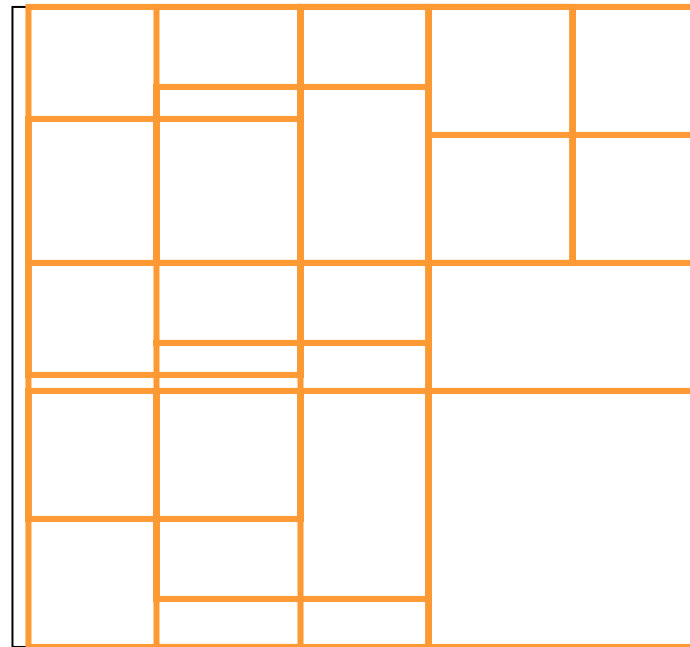
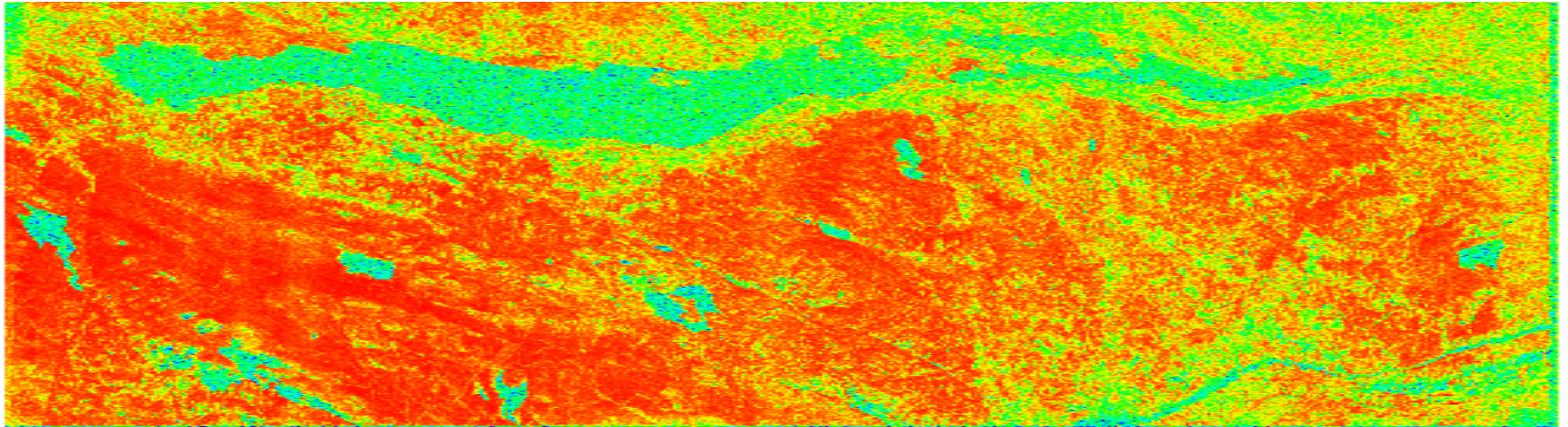
Application of Edge aligned Lee Filter to each Scattering group



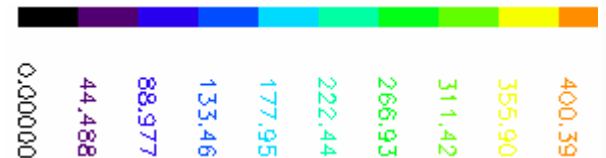
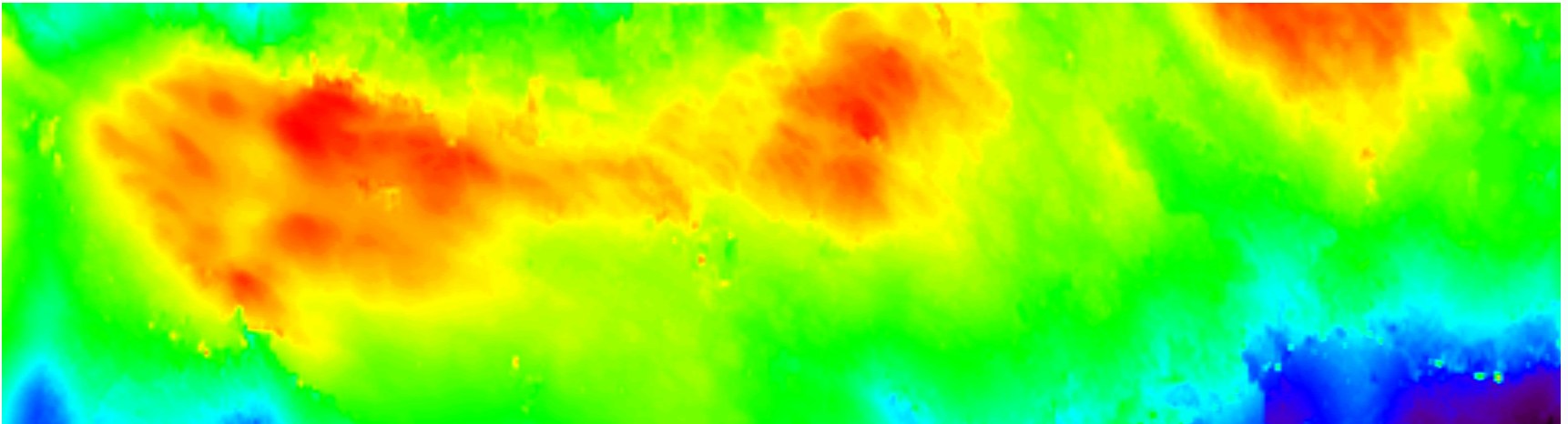
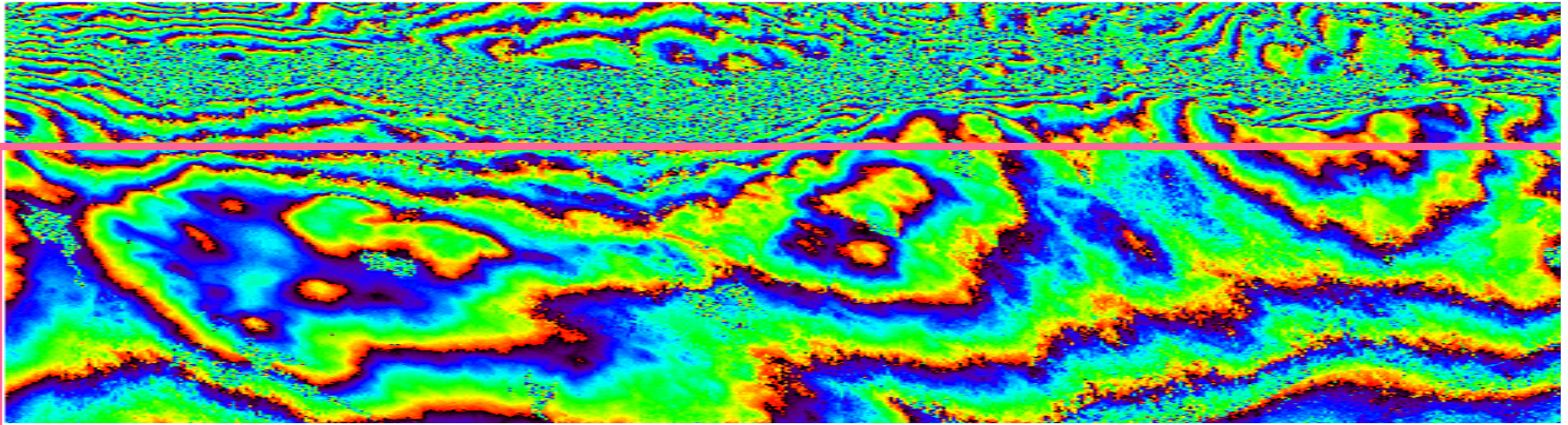
ESPRIT algorithm

Interferogram for the dominant eigen parameter

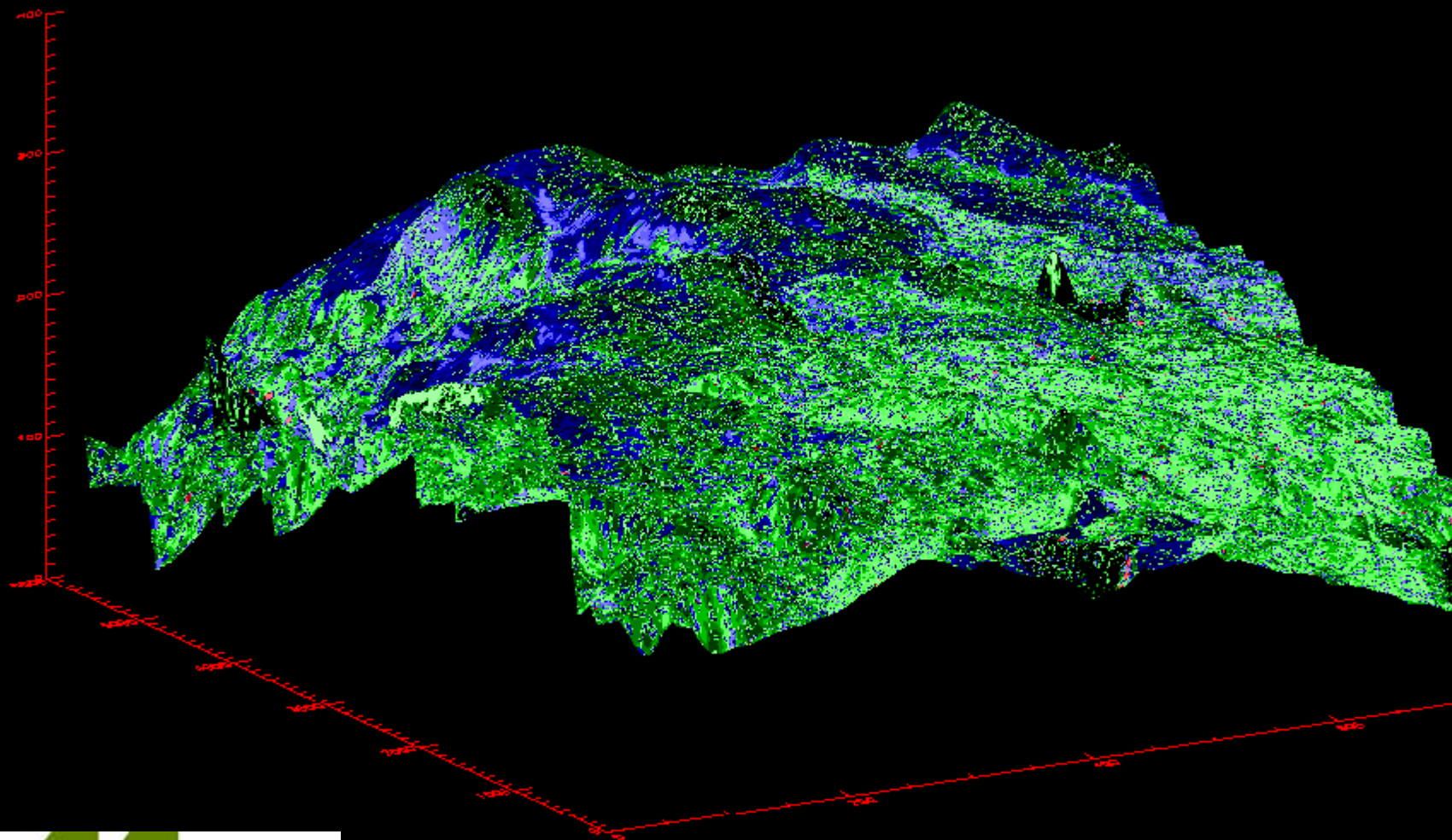
Phase Unwrapping Solution



Digital Elevation Model

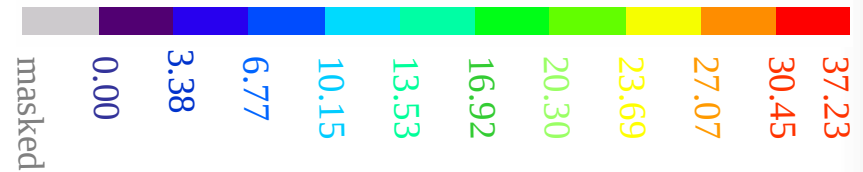
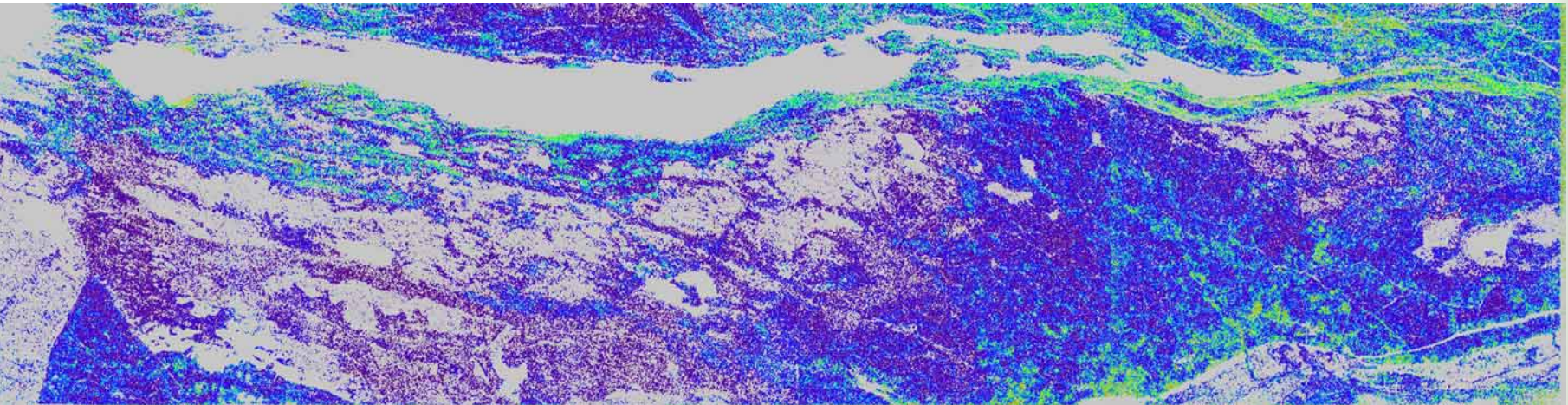


Digital Elevation Model

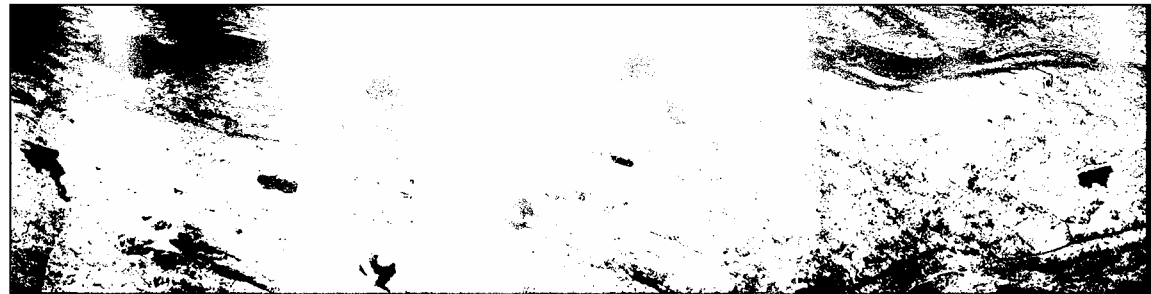


Glenaffric Tree Height

ESPRIT



Temporal de-correlation
mask, 10m baseline
tracks, tree heights
of 45 m



Temporal de-correlation mask of Glen Affric radar data

Summary

Land Cover classification

(Freeman-Durden, Lee Filter, Wishart Classifier)

Temporal Decorrelation mask, SNR mask and Water mask

Interferometric Target Vector and Coherence matrix

Edge aligned enhanced Lee filter

TLS ESPRIT

DEM and Tree height